



Similitude in Sediment Transport Processes

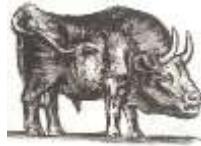
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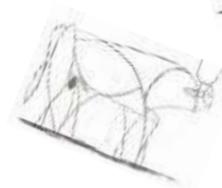
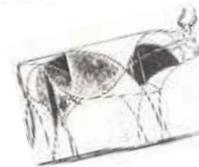


Institut national des sciences appliquées INSA, Lyon, February 16th, 2018



Outline

- 1.- Relevance / Motivation / Background
- 2.- Modelling the sediment transport
- 3.- Modelling the bridge pier scour



Relevance / Motivation / Background

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Proyectos de ingeniería sostenible



To build physical scale models of complex situations without known solution



To develop formulas from laboratory experiments for estimation of key parameters, such as the scour depth around piles

Relevance / Motivation / Background

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Identic





Similar





Distorted





Heller, V. (2011). Scale Effects in Physical Hydraulic Engineering Models. *Journal of Hydraulic Research*, 49(3), 293-306.

Heller, V. (2017). Self-similarity and Reynolds number invariance in Froude modelling. *Journal of Hydraulic Research*, 55(3), 293-309.

Dimensional analysis and similitude theory

Fluid: density, viscosity

Flow: gravitational acc., velocity, depth

$$f(\rho, \mu, g, u_{ef}, h, d_s, \rho_s, D, t, z) = 0$$

Sediment: size, density

Obstacle: Length scale

Time

A variable of interest: i.e. scour depth

$$f\left(Re', Fr', \rho', \frac{h}{d_s}, \frac{D}{d_s}, \frac{u_{ef}t}{d_s}, \frac{z}{d_s}\right) = 0$$

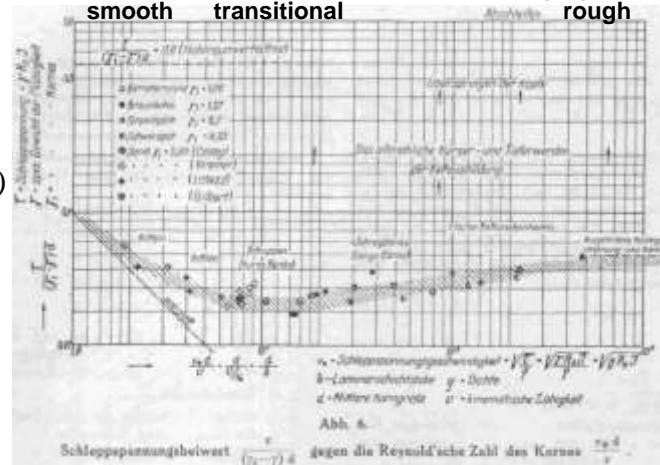
→ It is impossible to have identic *Re* and *Fr* in prototype and scale model

$$\lambda_{Re} \neq \lambda_{Fr} = 1$$

→ Scale effects arise

Buckingham, E. (1914). On physically similar systems; illustrations of the use of dimensional equations. Physical review, 4(4), 345.

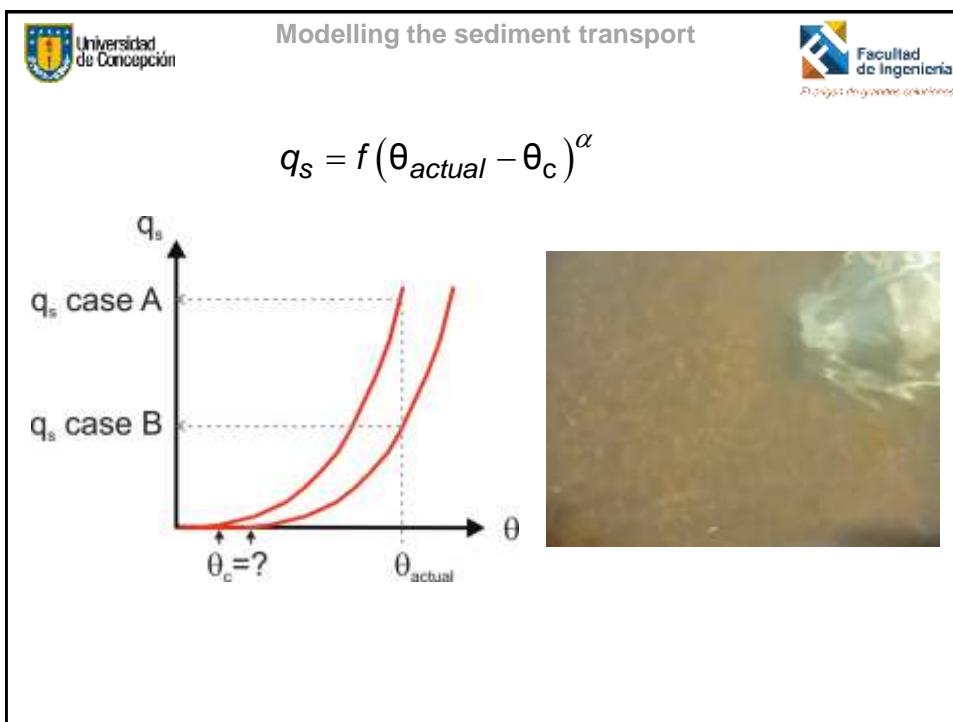
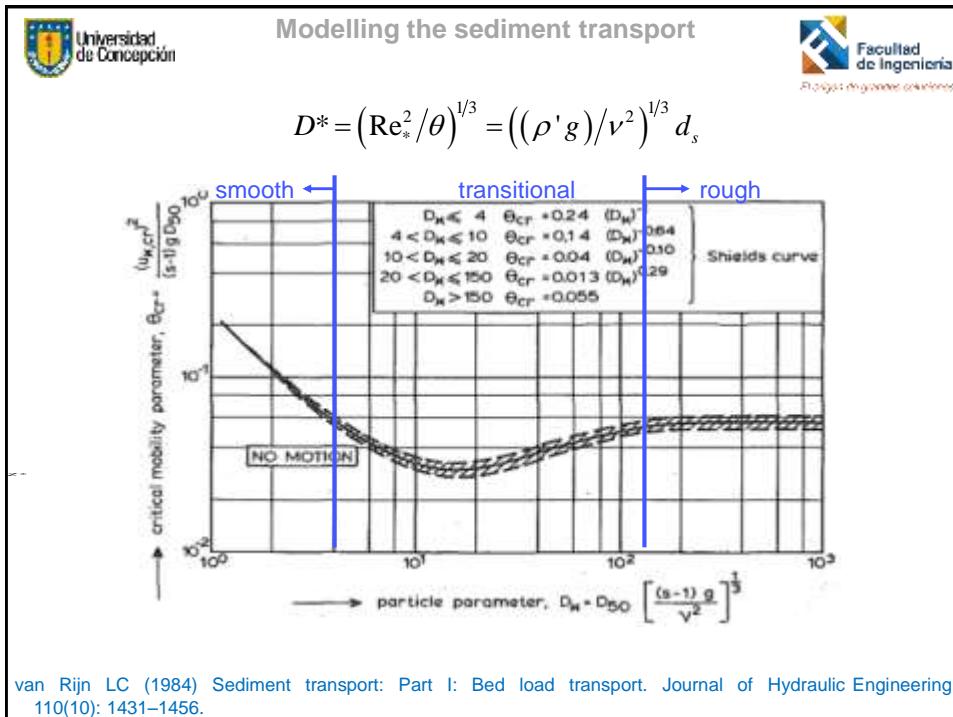
$$\theta_{cr} = \frac{u_*^2}{\rho' g d} = f(Re_*)$$



Shields A (1936) Anwendung der Ähnlichkeitsmechanik und der Turbulenzforschung auf die Geschiebewegung. PhD Thesis. TU Berlin.

Mantz PA (1977) Incipient transport of fine grains and flakes by fluids-extended shield diagram. Journal of the ASCE Hydraulics Division, 103(12992).

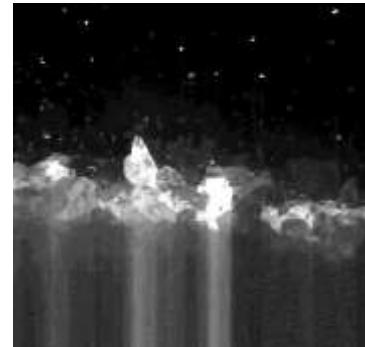
Yalin MS & Karahan E (1979) Inception of sediment transport. Journal of the ASCE Hydraulics Division, 105(11): 1433-1443.



A flow producing the same sediment behavior is needed, but taking Fr similarity...

$$\lambda_{Fr} = 1 \quad \lambda_g = 1:100$$

$$\frac{u_m}{\sqrt{gh_m}} = \frac{u_p}{\sqrt{gh_p}}$$



Video: Prof. M.Schmeeckle,
<http://www.public.asu.edu/~mschmeec/>

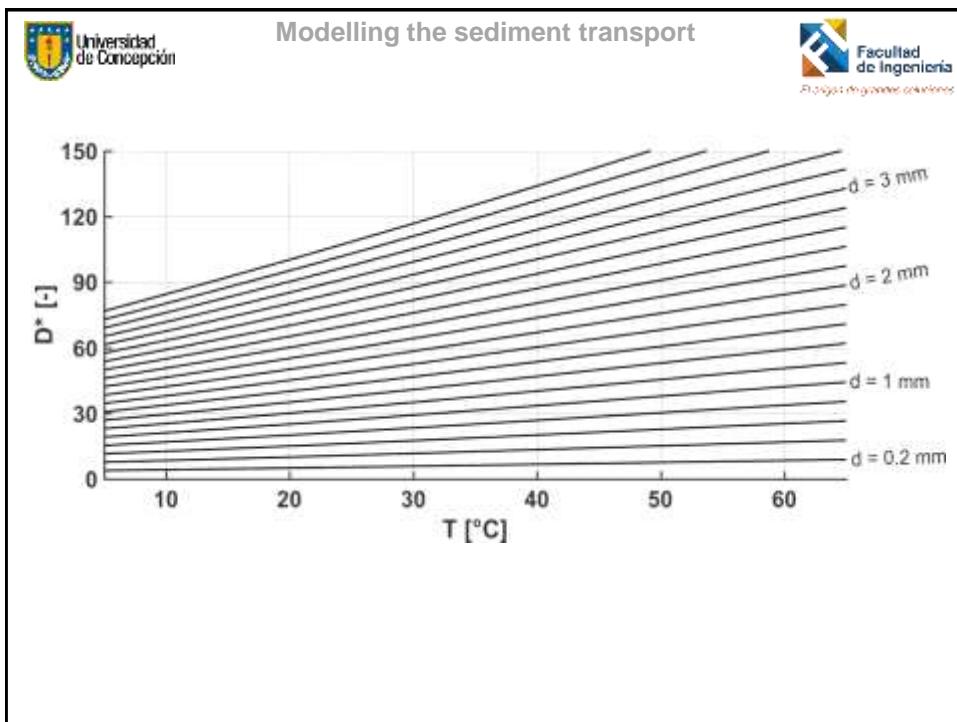
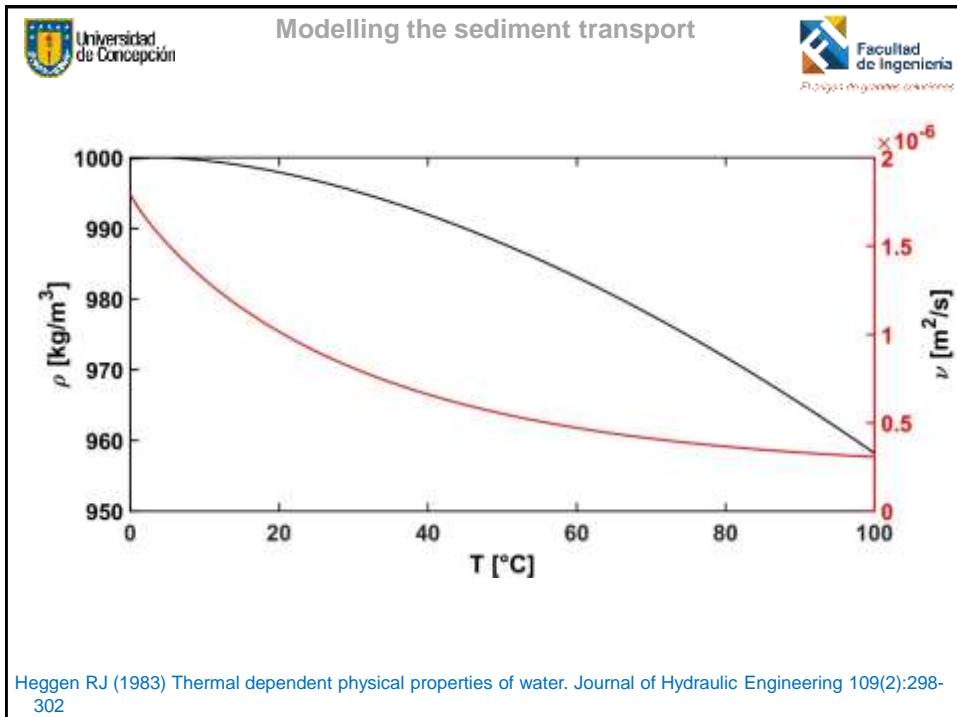
$$\rightarrow u_m = u_p \sqrt{\lambda_g} \approx 0.1u_p$$

We can't use the same sediment in model and prototype

Lightweight material	d_s (mm)	Specific gravity (-)	D^* (-)	Equivalent sand (mm)
Acrylonitrile butadiene styrene (ABS)	2.3-3.0	1.22	30-39	1.18-1.53
Bakelite	0.35-4.0	1.30-1.45	5-66	0.2-2.59
Coal	0.1-40.0	1.37-1.61	1.5-726	0.06-28.70
Lightweight Aggregate	1.0-3.0	1.70	19-57	0.75-2.25
Perspex	0.3-1.0	1.18-1.19	3.6-12.3	0.14-0.49
Polyamidic Resins (Nylon)	0.1-5.0	1.16	1.2-58.1	0.05-2.30
Polystyrene	0.5-3.2	1.035-1.05	3.5-25.2	0.14-1.00
PVC	1.5-4.0	16.70	16.7-53.9	0.66-2.13
Sawdust treated with Asphalt	0.6-1.0	1.05	4.7-7.9	0.19-0.31
Sand of Loire	0.63-2.25	1.50	10.7-38.2	0.42-1.51
Walnut Shells, Ground	0.15-0.41	1.33	2.2-6.1	0.09-0.24
Granulated Obeche wood	0.8	1.10	7.9	0.31



Bettess, R. (1990). Survey of lightweight sediments for use in mobile-bed physical models. in *Movable Bed Physical Models* (pp. 115-123). Springer, Netherlands.



Is it incipient motion or not?

Classic criteria:

Kramer (1932, 1935)

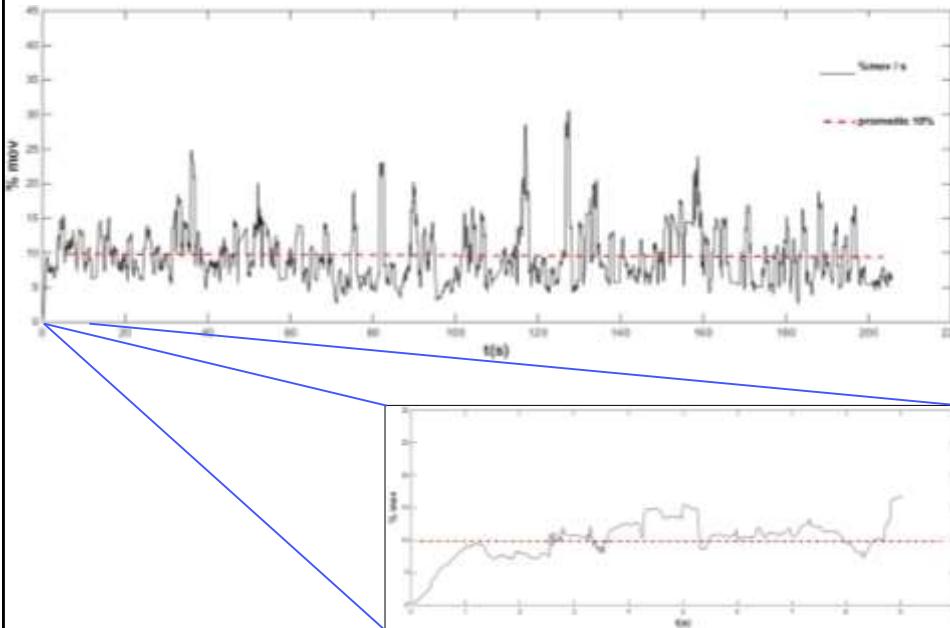
US WES (1935)

Shields (1936)

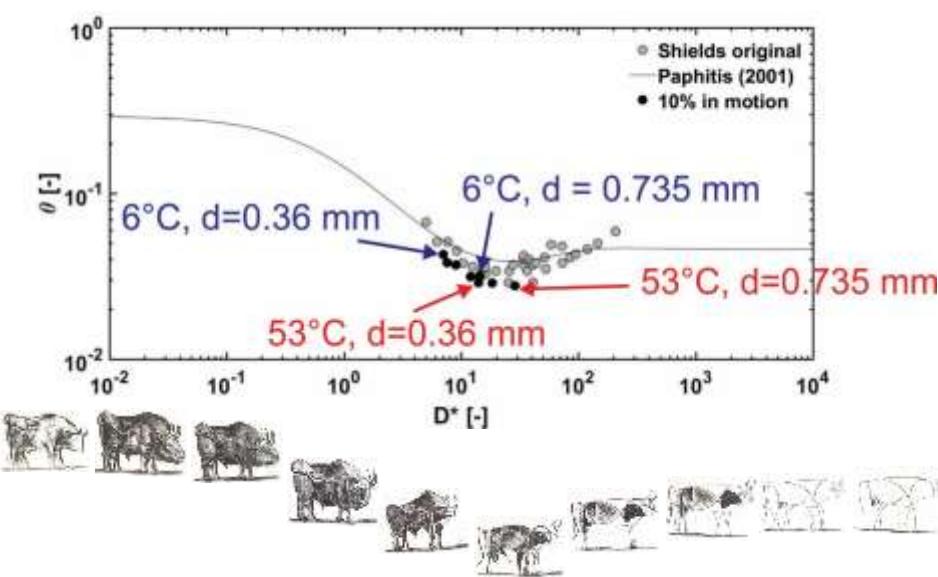
Keshavarzy & Bell (1999): ~10%

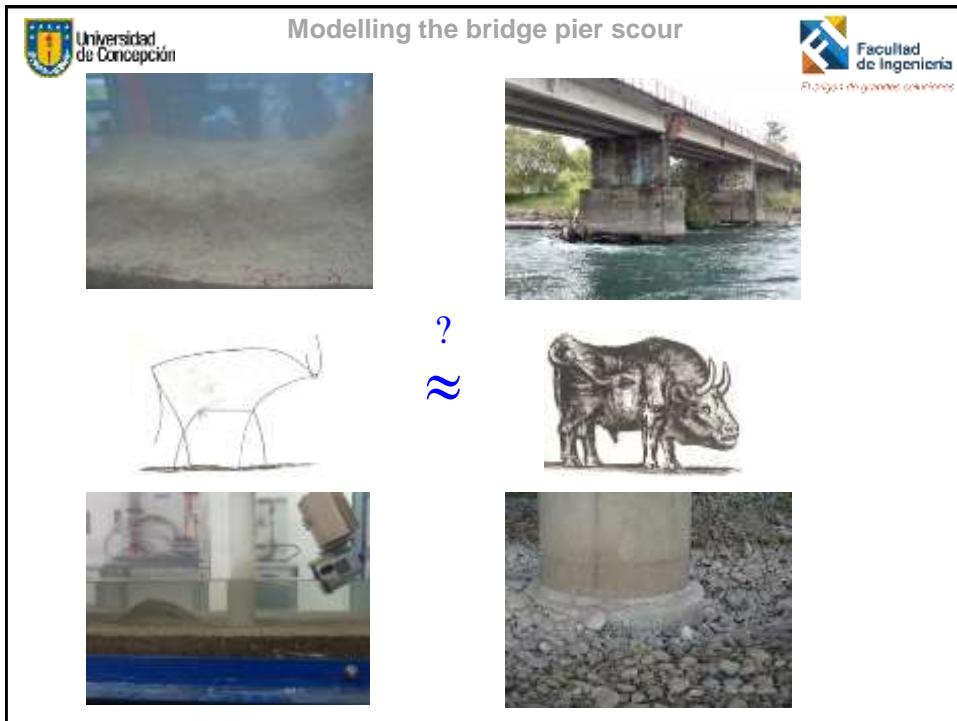


Keshavarzy A & Bell JE (1999) An application of image processing in the study of sediment motion. Journal of hydraulic research, 37(4): 559-576.



Serie experimental_Estado mov [$d_{50} = 0.36 \text{ mm}$]						
Serie 1(T°)	Ensayo N°	h (cm)	$Q_c (\text{l/s})$	$U_c (\text{cm/s})$	%mov	Cond. Incipiente
6°C	E1	12	15.5	32.05	9.0%	
	E2	12	15.8	32.67	10.4%	OK
10°C	E1	12	15.0	31.02	10.2%	OK
	E2	12	15.5	32.05	11.5%	
20°C	E1	12	15.0	31.02	10.0%	OK
	E2	12	15.5	32.05	12.0%	
40°C	E1	12	13.5	27.92	8.0%	
	E2	12	14.0	28.95	9.8%	OK
53°C	E1	12	13.8	28.54	10.2%	OK
	E2	12	13.5	27.92	8.0%	





Modelling the bridge pier scour

$f(\mu, \rho, u_{ef}, h, g, d_s, \rho_s, D, t, z) = 0$

$$f\left(\text{Re}', \text{Fr}', \rho', \frac{h}{d_s}, \frac{D}{d_s}, \frac{u_{ef}t}{d_s}, \frac{z}{d_s}\right) = 0$$

"The use of laboratory flumes in developing accurate predictors of scour depth at full-scale piers is limited due to scale effects that may produce greater scour depths at the laboratory than at actual piers in rivers" (Ettema et al. 1998)

Ettema et al.(1998) Scale Effect in Pier Scour Experiment. J. of Hydraulic Engrg. 124(6):639-642.
 Ettema et al. (2006) Similitude of Large-Scale Turbulence in Experiments on Local Scour at Cylinders. J. of Hydraulic Engrg. 132(1):33-40.
 Cheng et al. (2016) Scaling Analysis of Pier-Scouring Processes. J. of Engrg Mechanics. DOI: 10.1061/(ASCE) EM.1943-7889.0001107



Modelling the bridge pier scour

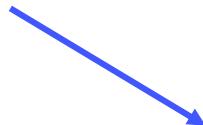


$$D^* = \left(Re^2 / (Fr_d'^2 / \rho') \right)^{1/3} = ((\rho' g) / v^2)^{1/3} d_s$$

$$Fr_d = Fr'(\rho')^{-0.5} = u_{ef} / \sqrt{\rho' g d_s}$$

$$U^* = 2(u_{ef} t / d_s) (D/d_s)^{-2} = u_{ef} t / (D^2 / 2d_s) = u_{ef} t / z_R$$

$$Z^* = (z/d_s) (D/d_s)^{-1} = z/D$$



$$Z^* = f \left(D^*, Fr_d, \rho', \frac{h}{d_s}, \frac{D}{d_s}, U^* \right)$$

Pizarro A, Ettmer B, Manfreda S, Rojas A & Link, O. (2017) "Dimensionless, Effective Flow Work for Estimation of Pier Scour caused by Flood Waves". Journal of Hydraulic Engineering. 143(7):1-7.
 Link O, Castillo C, Pizarro A, Rojas A, Ettmer B, Escuinaza C & Manfreda S. (2017) "A model of bridge pier scour during flood waves". Journal of Hydraulic Research, 55(3):310-323.



Modelling the bridge pier scour



$$w \propto \tau_0 u \longrightarrow \tau_0 \propto \rho u^2 \longrightarrow w \propto u^3$$

$$w_{ef} \propto \int u_{ef}^3 \delta dt \quad \delta = \begin{cases} 0 & u/u_{cs} < 1.0 \\ 1 & u/u_{cs} \geq 1.0 \end{cases}$$

$$u_R = \sqrt{\rho' g d_s} \quad t_c = \frac{D^2}{2d_s u_{ef}}$$

$$W^* \propto \int_0^{t_{end}} \frac{1}{t_c} \left(\frac{u_{ef}}{u_R} \right)^3 \delta dt = \int_0^{t_{end}} \frac{u_{ef}}{(D^2 / 2d_s)} \left(\frac{u_{ef}}{u_R} \right)^3 \delta dt = \int_0^{t_{end}} Fr_d^3 \frac{u_{ef}}{z_R} \delta dt$$

$$W^* \propto \int_0^{t_{end}} Fr_d^3 \frac{u_{ef}}{z_R} \delta dt$$

Bagnold (1966); Lai et al. (2009); Oliveto & Hager (2002); Guo (2014)

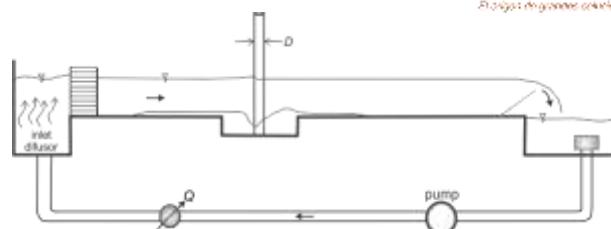
Hypothesis: $Z^* = f\left(W^*, D^*, \frac{D}{d_s}\right)$

Similitude: $\lambda_{Z^*} = \lambda_{W^*} = \lambda_{D^*} = \lambda_{D/d_s} = 1$

Time scale: $\lambda_t = \left(\frac{u_{ef,p}}{u_{ef,m}}\right)^4 \left(\frac{D_m}{D_p}\right)^2 \left(\frac{\rho'_m}{\rho'_p}\right)^{3/2} \left(\frac{d_{sm}}{d_{s,p}}\right)^{1/2} = \lambda_{u_{ef}}^{-4} \lambda_D^2 \lambda_{\rho'}^{3/2} \lambda_{d_s}^{1/2}$

Link O, Henríquez S & Ettmer B (2018) Physical scale modelling of scour around bridge piers. Journal of Hydraulic Research, (accepted for publication).

	D	B
Flume 1	0.150	1.4
Flume 2	0.046	0.4
Flume 3	0.030	0.3



	d _s (mm)	ρ (t/m ³)	D*
Sand 1	0.36	2.65	9
Sand 2	0.74	2.65	18
Sand 3	0.80	2.65	21
Sand 4	1.60	2.65	40
Acetal	2.60	1.39	41
Polystyrene	2.74	1.04	20

5 Series with 17 experiments:

- S1: same sediment, unsteady Q
- S2: sand vs polyst, clear-water and live -bed
- S3: sand vs polyst, steady Q up to eq. scour
- S4: different flow intensities to test time scale
- S5: different D / d_s to test scale effects

